

Worksheet Standard Deviation

X: 60 61 61 62 62 62 62 63 63 64

Mean: 62

Median: 62

Midrange: $\frac{60 + 64}{2} = 62$

Mode: 62

$$\frac{62 + 62}{2} = 62$$

X	$x - \bar{x}$	$(x - \bar{x})^2$
60	-2	4
61	-1	1
61	-1	1
62	0	0
62	0	0
62	0	0
62	0	0
62	0	0
63	1	1
63	1	1
64	2	4

$$\sum (x - \bar{x})^2 = 12$$

$$s^2 = \frac{\sum (x - \bar{x})^2}{n - 1}$$

$$= \frac{12}{9}$$

$$= 1.\bar{3}$$

$$s = \sqrt{1.\bar{3}}$$

$$\approx 1.15$$

$$\bar{x} = 62$$

X	x^2
60	3600
61	3721
61	3721
62	3844
62	3844
62	3844
62	3844
62	3844
63	3969
63	3969
64	4096

$$\sum (x^2) = 38,452$$

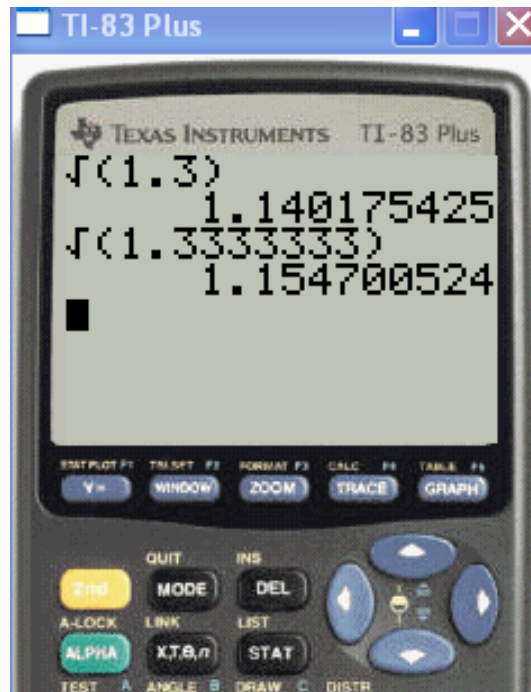
$$s^2 = \frac{\sum x^2 - \frac{(\sum x)^2}{n}}{n - 1}$$

$$= \frac{38452 - \frac{(620)^2}{10}}{9}$$

$$= \frac{38452 - 38440}{9}$$

$$= 1.\bar{3}$$

$$s \approx 1.15$$



Notice - rounding too soon gives much rounding error in answer.

3.45

6 3 7 11 4 3 8 7 2 6 9 15

range $15 - 2 = 13$ range

$$\text{mean} = \frac{\sum x}{12} = \frac{81}{12} \approx 6.75$$

x	x^2
6	36
3	9
7	49
11	121
4	16
3	9
8	64
7	49
2	4
6	36
9	81
15	225
<hr/>	
81	699

$$s^2 = \frac{\sum x^2 - \frac{(\sum x)^2}{n}}{n-1}$$
$$= \frac{699 - \frac{(81)^2}{12}}{11}$$
$$= \frac{699 - \frac{6561}{12}}{11}$$
$$= \frac{699 - 546.75}{11}$$

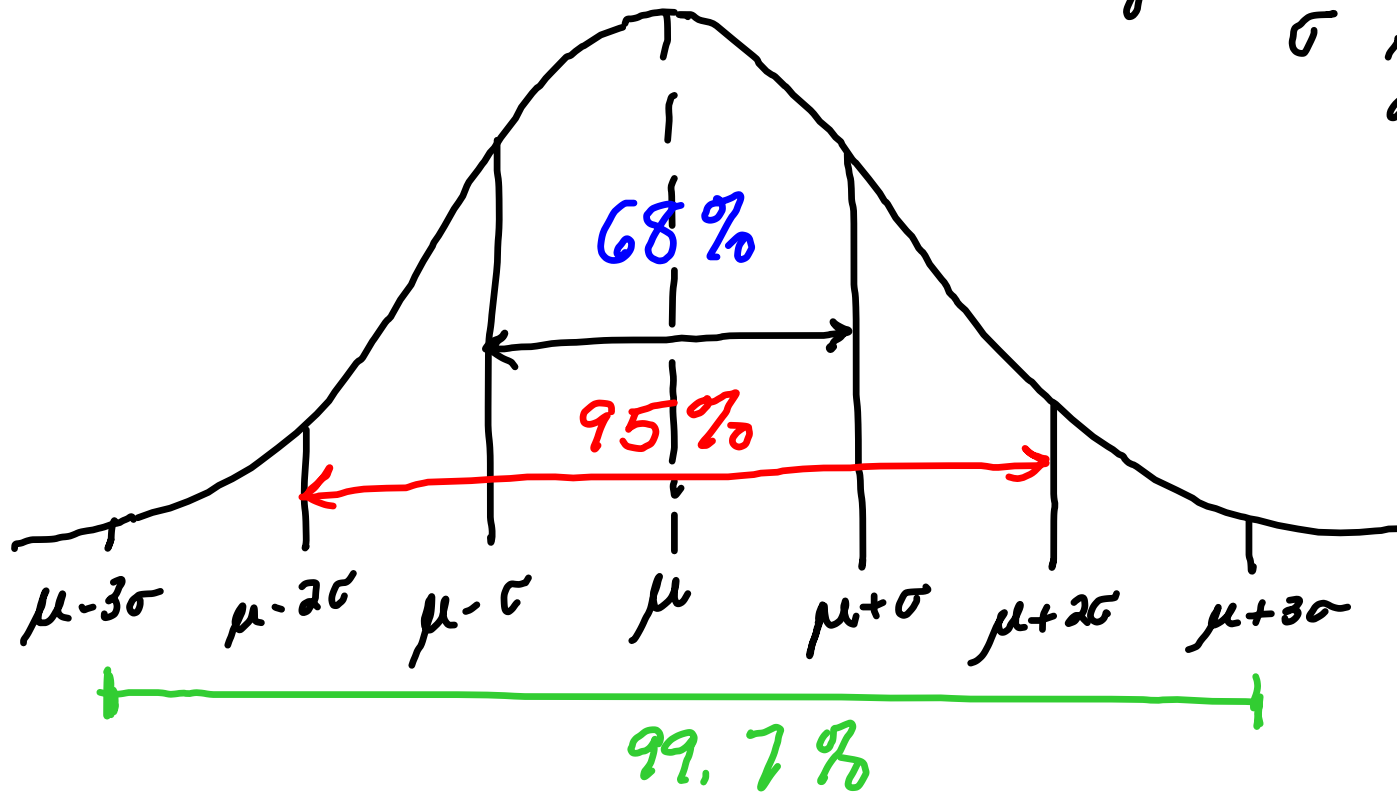
$$s^2 \approx 13.8409$$

$$s \approx \sqrt{13.8409}$$

$$s \approx 3.72$$

The Empirical Rule

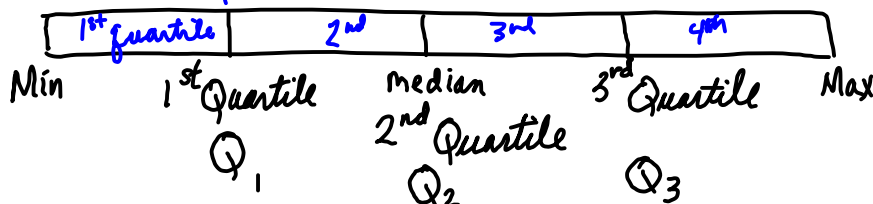
Symmetric
 σ standard deviation



8.5 Measures of Position

Quartiles IQR

Where is 60 grams?



$$\text{IQR} - \text{Interquartile Range} = Q_3 - Q_1$$

Look at kittens

37	38	40	41	44	45	49	51	52	52	54	56	57	57	58
					↓							Q ₂		
					↓									
60	63	63	65	69	72	76	77	84	91					

Q₂ $\frac{n+1}{2} = \frac{25+1}{2} = 13$ this is where it is
median Q₂ is actually 57

$$Q_1 \quad \frac{12+1}{2} = \frac{13}{2} = 6.5$$

$$\frac{45+49}{2} = 47$$

$$Q_3 \quad \frac{65+69}{2} = 67$$

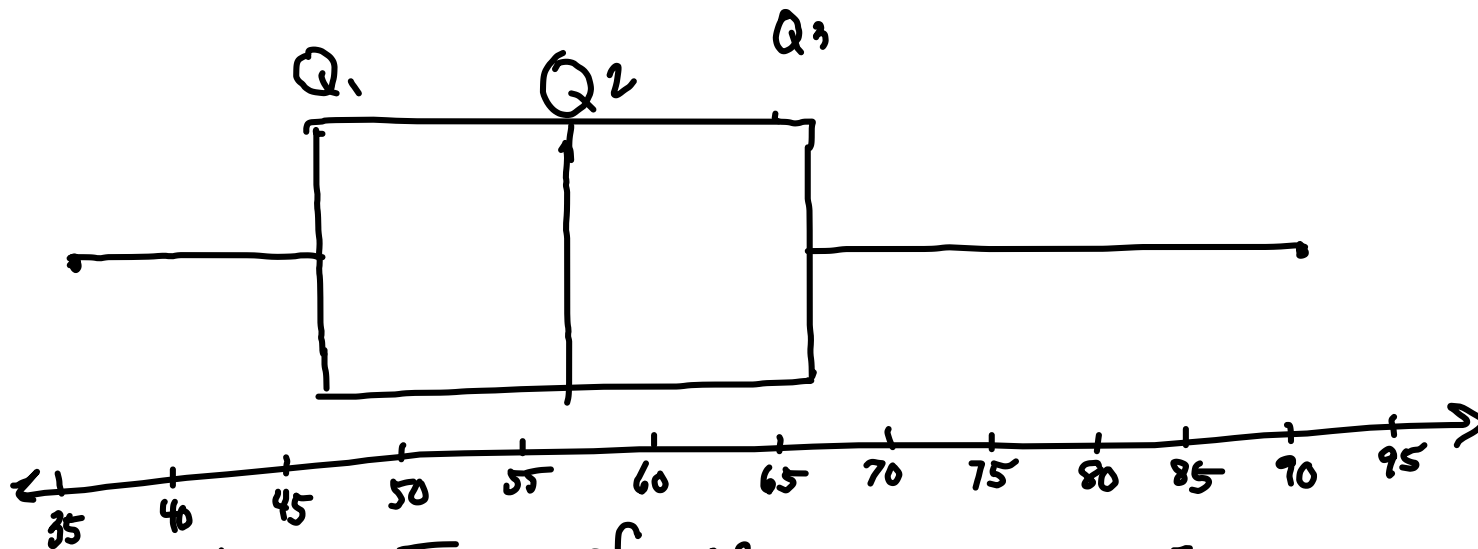
$$\text{IQR} = 67 - 47 = 20$$

Between 47 and 67 we have
50%

Five number summary

Min 37 Q_1 47 Q_2 57 Q_3 67 Max 91

Box & Whisker Plot



Lower Inner fence

$$f_L = Q_1 - 1.5(IQR) = 17$$

$$f_U = Q_3 + 1.5(IQR) = 97$$

Upper Inner fence

Test
next Tuesday
2/14/2012
Chapters 2 & 3